

# Optimization of Piezoelectric Energy Harvesting Systems by Using a MPPT Method

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**Abstract**— This paper proposes an optimization of a piezoelectric energy harvesting system by using a maximum power point tracking (MPPT) method. A full-bridge rectifier is implemented with a MPPT unit to obtain maximum extracted power by controlling a DC-DC converter following the rectifier. By using the MPPT unit, the extracted power efficiency of the rectifier is always larger than 80% regardless of the load condition. Furthermore, another DC-DC converter is applied to regulate the output voltage to the desired level. The simulation results show that the system can extract a maximum of 51  $\mu$ W power with 64% total efficiency.

**Keywords**- AC-DC converter, MPPT, rectifier, piezoelectric energy harvesting system.

## I. INTRODUCTION

Energy harvesting is becoming increasingly important in our lives. Energy can be harvested from the ambient environment, including mechanical, thermal, light, and electromagnetic sources, the human body, and others, to replace traditional sources. Mechanical energy harvesting is the most promising energy harvesting technique: it uses piezoelectric (PE) component that transfer vibration energy to electrical energy. This electrical energy can be regulated and stored before being used by an electronic device. This is particularly useful in applications where the replacement of batteries is impractical, such as wireless micro-sensor networks, implementable medical electronics, and tire pressure sensor systems [1].

Fig.1 illustrates a general piezoelectric energy harvesting system that consists of five major components [2-4]. A transducer is a sensor PE transducer that deforms vibration energy into electrical energy. The PE transducer is usually modeled by an AC current source in parallel with a capacitor and a large resistor [1,2,4,5]. The electrical energy at the output of the transducer is a strong and irregular function of time; an AC-DC converter is hence required to produce a DC supply source. The energy after the rectifier is stored in an energy storage device such as a battery or supercapacitor. Before the system is used under load, normally a voltage regulator is operated to ensure suitable voltage.

A rectifier, which has been proposed and demonstrated in recent work, is the most commonly used AC-DC converter [1-5]. There are two types of conventional rectifiers: full-bridge rectifiers and voltage doubler rectifiers. The limitations of the

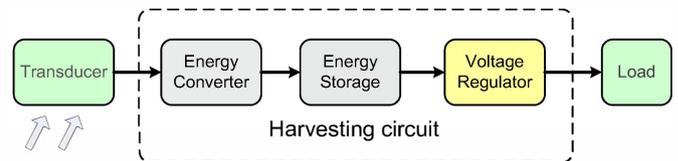


Fig. 1. A Piezoelectric energy harvesting system

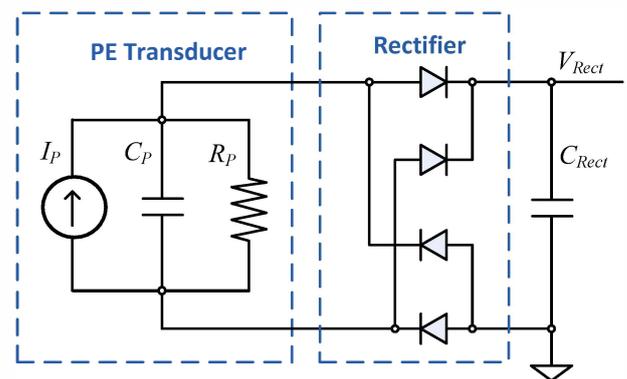


Fig.2 Piezoelectric transducer model and full-bridge rectifier

conventional architectures are low efficiency due to the voltage drop in each passive diode and power loss during discharging and charging for the internal capacitor [1-2]. There are two directions for improving the efficiency of power extracted from the PE transducer. The first approach is replacing the passive diode with an active diode to reduce the voltage drop in each diode. The second approach is improving the efficiency of the conventional rectifier by resetting [1,2,5] or flipping [2,5] the internal capacitor when the internal current source of the transducer crosses zero. However, the extracted power in the previous rectifier [1-5] depends on the load condition. The rectifiers can only obtain high extracted power efficiency at a small range of output load resistance. If the load resistance is outside of this range, the extracted power of the rectifier is significantly reduced. The MPPT method is used to extract more power in a PE energy harvesting system in [6]. However, in this study MPPT is implemented by using a MCU –TI eZ430-RF2500, and therefore the area and cost are significantly increased.

In this study, a MPPT unit is added to the rectifier to ensure that the system always obtains maximum extracted power despite load variation. The MPPT is used in this paper can be

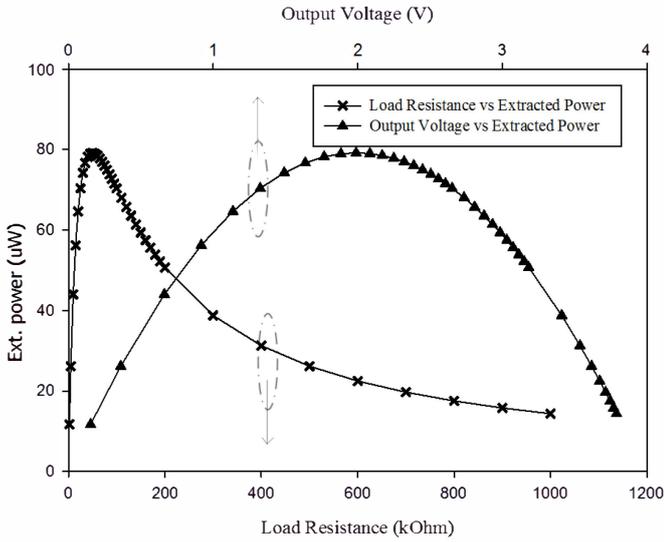


Fig.3. Extracted power of conventional rectifier

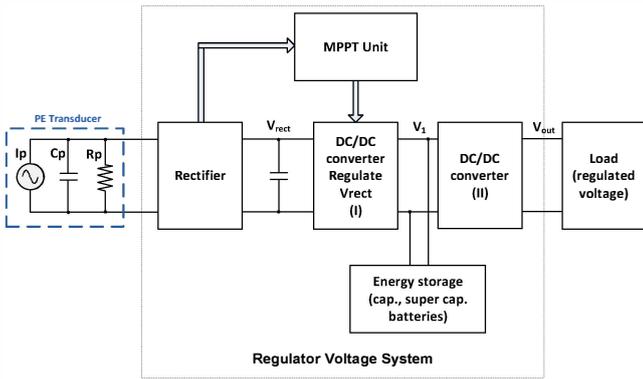


Figure 4. The proposed piezoelectric energy harvesting system.

integrated in system. Furthermore a full system for piezoelectric energy harvesting also introduces in this paper.

This paper is organized as follows. Section II proposes an architecture for the PE energy harvesting system with a MPPT unit. Section III provides the simulation results and a discussion of the proposed system. Finally, Section IV briefly concludes this paper.

## II. ARCHITECTURE OF PEH SYSTEM

As shown in the left side of Fig.2, a PE transducer is usually modeled as a sinusoidal current source  $i_p(t) = I_p \sin 2\pi f_p t$ , in parallel with a capacitor  $C_p$  and a large resistor  $R_p$ . The magnitude of the PE current,  $I_p$ , varies with the mechanical excitation level of the PE element, although it is assumed to be relatively constant regardless of the external load;  $f_p$  is the excited frequency of the PE harvester [1]. The output of the transducer has an AC waveform, which must be converted to DC by an AC-DC rectifier before it can be transferred to the battery or supercapacitor.

Several techniques have been proposed to improve extracted power by resetting or flipping the internal capacitor [1,2,5] when the internal current source crosses zero [2,5]. Although the reported techniques improve the maximum

extracted power, the range of output load resistance to obtain high extracted power is narrow. Thus, if the load resistance is outside of this narrow range, the efficiency of system will be significantly reduced.

For the conventional full-bridge rectifier, as shown in Fig. 2, the extracted power Eq. (1) and maximum extracted power Eq. (2) are given by [2] with the assumption that the voltage drop in each active diode is zero.

$$P_{out} = 4C_p f_p (V_{OC} - V_{rect}) V_{rect} = \left( \frac{4C_p f_p V_{OC} \sqrt{R_L}}{1 + 4C_p f_p \sqrt{R_L}} \right)^2 \quad (1)$$

$$P_{out, maximum} = C_p f_p V_{OC}^2 \quad (2)$$

where  $V_{oc} = \frac{I_p}{2\pi C_p f_p}$  is the open circuit voltage of the

rectifier.  $V_{rect}$  is the output voltage of the rectifier and  $R_L$  is the load resistance. The output voltage obtains maximum extracted power when  $V_{rect} = V_{rect, opt} = V_{OC}/2$  or the load resistance at

$$R_{L, opt} = \frac{1}{4C_p f_p}. \text{ Eq.(2) shows the extracted power of the}$$

rectifier is a function of the load resistance. The extracted power is only maximal at one point when the load resistance equals  $R_{L, opt}$ .

Fig. 3 shows the function of the extracted power  $P_{out}$  with the output voltage and load resistance, as expressed in Eq. (1) and Eq. (2) with the following input PE transducer parameters:  $I_p = 125 \mu A$ ,  $f_p = 200 \text{ Hz}$ ,  $C_p = 25 \text{ nF}$ , and  $R_p = 1 \text{ M}\Omega$ . The output power is high in a small range of load resistance from 70K $\Omega$  to 130K $\Omega$ , and the extracted power is reduced significantly when the load resistance changes. However, in a real system, the load is continuously changing, and thus the system cannot operate only in the maximum point area. If the system operates with small or large resistance load, the extracted power of the rectifier is very small. Fig. 3 also illustrates that the maximum extracted power of the rectifier is only obtained in a small area of  $V_{rect}$  from 1.5V to 2.5V. If the value of  $V_{rect}$  is outside of that range, the efficiency of the system will be significantly reduced. To improve the efficiency of the system, a PE energy harvesting system with MPPT is proposed in this paper. The MPPT is designed to regulate the output voltage of the rectifier,  $V_{rect}$ , by an active or inactive DC-DC (I) converter following the rectifier.

### A. Proposed Optimized PE Energy Harvesting System

Fig. 4 shows the proposed PE energy harvesting system. A PE transducer is connected to the full bridge rectifier to change the AC waveform to a DC waveform. A DC-DC converter (I) follows the rectifier to regulate  $V_{rect}$ . The operation of the DC-DC converter (I) is controlled by the MPPT unit. The MPPT unit monitors the output voltage of the rectifier and then adjusts the duty cycle of the DC-DC converter (I) to set the output voltage at the output of the rectifier at the optimum value,  $V_{rect, opt}$ . Because the output voltage of the rectifier is regulated at  $V_{rect, opt}$ , the output voltage at  $V_1$  can be larger or smaller than  $V_{rect}$ . The buck-boost converter is thus suitable for a DC-DC converter (I). The purpose of the DC-DC converter (I) is to

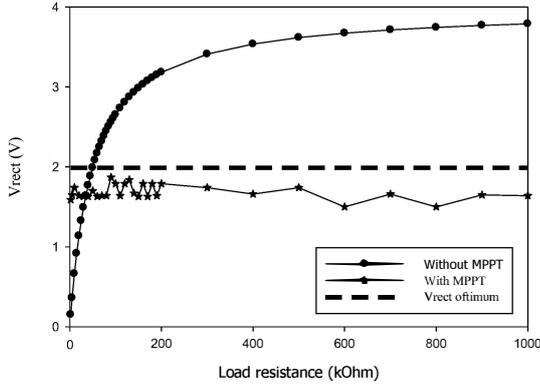


Figure 5. Comparison between  $V_{rect}$  of PE system with and without MPPT when load change from  $2k\Omega$  to  $1M\Omega$

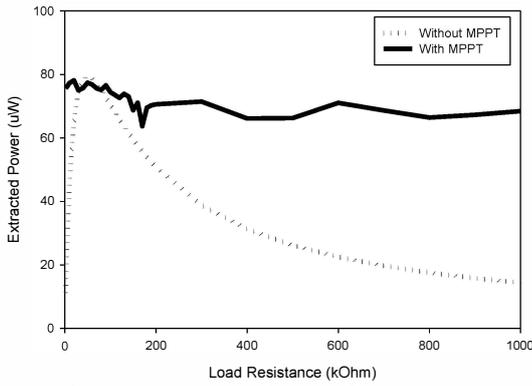


Figure 6. Comparison extracted power with and without MPPT

keep  $V_{rect}$  at the optimum value; the voltage at  $V_1$  is therefore not controllable. The second DC-DC converter is used for regulating the output voltage of the system at a desired level.

In comparison with the conventional PE energy harvesting shown in Fig. 1, a MPPT unit and a DC-DC converter are added to the system. The MPPT unit and DC-DC converter (I) help ensure that the rectifier always operates near the optimum range of  $V_{rect}$  to derive high extracted power.

### B. Rectifier and MPPT Unit.

The first block of the regulator voltage system is the rectifier. With implementation of a full-bridge rectifier, the AC waveform of the transducer is deformed to a DC waveform. To reduce the power loss across the rectifier, all diodes in the rectifier are implemented as active diodes to reduce the voltage drop. Because the excited frequency of the PE harvester is small (smaller than 1000Hz) the active diodes can be implemented by a transistor and one comparator. By adopting the active diode, the voltage drop in each diode is reduced from 400mV to 10 mV.

The MPPT unit is implemented to detect the maximum extracted power point in Fig.3, and to control the rectifier operating at the optimum  $V_{rect,opt}$ . At the optimum  $V_{rect,opt}$ , the rectifier can extract the maximum output voltage. The MPPT is designed by monitoring the change of  $V_{rect}$ . As mentioned before, the optimum value of  $V_{rect}$  equals half of  $V_{OC}$ . The proposed system uses a MPPT to detect  $V_{OC}$  every 2 minutes.

To obtain the value of  $V_{OC}$ , the converter (I) is disabled. During detection of the  $V_{OC}$  period, the rectifier operates as an open circuit, and then the MPPT can obtain the  $V_{OC}$  value of the rectifier. This value is stored in one capacitor and used as the reference voltage of  $V_{rect}$ . By monitoring the change of  $V_{rect}$ , the MPPT controls the DC-DC converter (I) to regulate  $V_{rect}$  at the optimum value ( $V_{OC}/2$ ).  $V_{rect}$  is controlled by the DC-DC converter (I); when  $V_{rect}$  is larger than  $V_{rect,opt}$ , the DC-DC converter (I) is activated, and conversely it is deactivated when the value is smaller. The time for sampling the value of  $V_{OC}$  is 20ms. During the detection period value of  $V_{OC}$ , the system operates by reserve energy from energy storage.

As mentioned before, the DC-DC converter (I) is implemented by a buck-boost converter; the conversion ratio of the converter is given by:

$$V_{out} = -\frac{D_1}{1-D_1} V_{in} \quad (3)$$

where  $D_1$  is the duty cycle of the DC-DC converter, and  $V_{out}$  and  $V_{in}$  are the output and input voltage of the converter at the steady state, respectively.

$D_1$  and  $V_{rect}$  move in opposite directions, where increasing  $D_1$  causes increased power flow to the output, and therefore  $V_{rect}$  will decrease. Conversely, if  $D_1$  decreases,  $V_{rect}$  will increase. In the system the value of  $V_1$  is not constant, and depends on the output power consumption and the duty cycle  $D_1$ .

### C. DC-DC Converter.

With use of MPPT,  $V_{rect}$  is kept at  $V_{rect,opt}$ , and therefore if the output load resistance at  $V_1$  is larger than  $R_{opt}$ ,  $V_1$  will be larger than  $V_{rect,opt}$ ; conversely, if the resistance at  $V_1$  is smaller than  $R_{opt}$ ,  $V_1$  will be smaller than  $V_{rect,opt}$ . Therefore, the range of  $V_1$  is larger than that of  $V_{rect}$ . For this reason, a buck-boost converter is suitable for DC-DC converter (I). The duty cycle of the DC-DC converter (I) is controlled by MPPT to ensure the rectifier operates at the optimum point. In the system, a simple buck-boost converter is operated with a switching frequency of 100kHz, and the duty cycle depends on the load condition.

The task of DC-DC converter (I) is to regulate  $V_{rect}$ , and therefore it cannot regulate the output voltage  $V_1$ . DC-DC converter (II) is added to regulate the output voltage at a level suitable to the desired voltage of the system. Because the output power of the PE energy harvesting is very small the entire design must minimize quiescent current. On this basis one more switch capacitor is used as the second DC-DC converter. The switch capacitor architecture optimizes power loss of the control circuit, and a hysteresis comparator defines the ripple of the output voltage.

## III. SIMULATION RESULTS

The system was simulated with the following transducer parameters:  $I_p=125 \mu A$ ,  $f_p=200$  Hz,  $C_p=25$  nF, and  $R_p=1$  M $\Omega$ . Under the same input conditions, the load resistor changes from  $2k\Omega$  to  $1M\Omega$ . With the simulation input parameters, from (2), the optimum value of  $V_{rect}$  ( $V_{rect,opt}$ ) equals to 1.98mV. Fig.5 shows a comparison of the output voltage of the rectifier

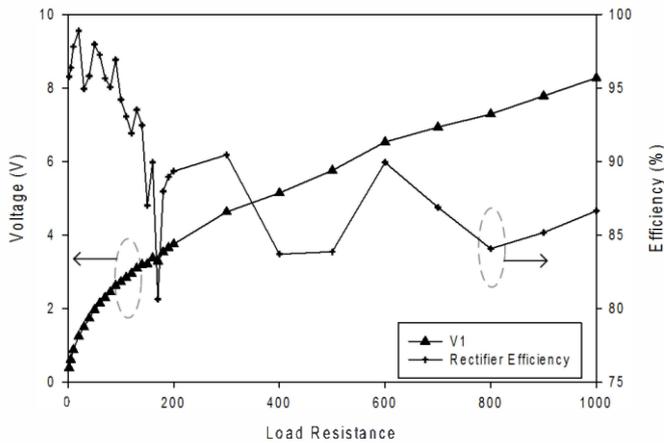


Fig. 7. Output voltage and output efficiency of the rectifier and DC-DC I

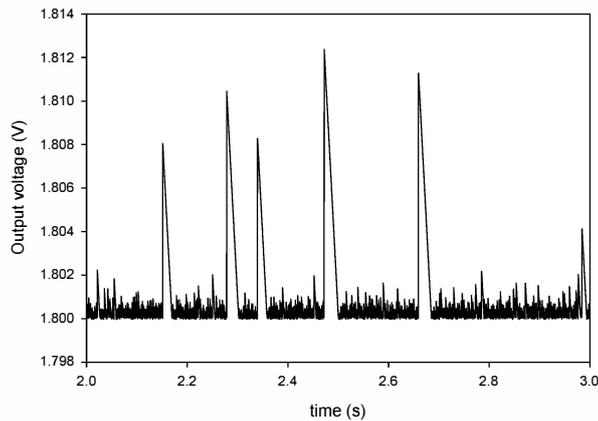


Fig. 8. Output voltage of system

with and without MPPT and the optimum value. The optimum value of  $V_{rect}$  is constant, while the value of  $V_{rect}$  without MPPT is an increasing function of load resistance, and there is a point where an optimum value is obtained. By adding the MPPT unit, the output voltage of the rectifier is always near the optimum value with respect to the load resistance. Because the rectifier operates in the optimum output value range, the system can extract more power.

Fig. 6 shows the extracted power of the rectifier with and without MPPT when the load condition is changed. Without MPPT, the shape of the extracted power is a function of the load resistance and the extracted power has efficiency larger than 90% at a small range of load from 25k $\Omega$  to 95K $\Omega$ , and outside of this range, the efficiency of the rectifier is low. Fig. 6 also illustrates that with MPPT, the output power of the extracted power is almost constant and is approximately equal to the maximum of the system without MPPT. The efficiency of the system with MPPT is larger than 90% in the full range from 2k $\Omega$  to 1M $\Omega$ .

Fig. 7 shows the output voltage at  $V_i$ , where the DC-DC converter at  $V_i$  only regulates the voltage for  $V_{rect}$ ; it does not control the output at  $V_i$ . With the same power, when the load resistance increases, the output voltage will also increase, as shown in Fig.7. The output efficiency of the rectifier is also shown in Fig. 7, where it is seen that the output efficiency is always larger than 80% regardless of the load resistance.

Fig. 8 shows the output voltage of the system with a 10 $\mu$ F output capacitor, and the output ripple of the system is about 12mV. The total efficiency of the proposed PE energy harvesting system is 64%.

#### IV. CONCLUSION

This paper has identified problems of rectifiers that are used in piezoelectric energy harvesting systems. The proposed system overcomes the drawbacks of previous rectifiers by adding a MPPT unit and one DC-DC converter. MPPT and the DC-DC converter help ensure that the rectifier always operates near the maximum area. The MPPT helps the transducer achieve power extraction efficiency that is always larger than 80%. With simple and efficient regulation of voltage, the overall efficiency of the piezoelectric system is 64%.

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